

# Distributed Algorithmics – TD2 - M2 IFI, Ubinet-CSSR, English version

## Exercise 1

1. What do the events  $p5$ ,  $q1$ ,  $p2$ ,  $r4$  represent ?
2. Looking at the diagram, can you tell if communication channels are FIFO or not ?
3. Looking at the diagram, can we have:
  - a. A sending of a message at  $q5$  and its reception at  $p2'$  ? (assuming  $q5$  and  $p2'$  are the events for this sending and reception, thus replacing those events actually shown on the diagram)
  - b. A sending of message at  $p3'$  and its reception at  $q3'$  ?
4. Apply Lamport clocks, initially at 0 on each process. What are the clock values on P after  $p6$ , on Q after  $q1$ , on R after  $r6$  ?
5. Give the minimum value of the whole execution. Assume that communication delay on a channel is bounded by  $\tau_{max}$
6. What are the events that cannot be compared (i.e. concurrent) to  $q6$ , according to the causality relation
7. Show that is 2 events  $a$  and  $b$  are such that  $clock(a) < clock(b)$ , we do not necessarily have that  $a$  precedes  $b$  according to the causality relation

## Exercise 2

We consider the temporal diagram (see figure 1), associated to the execution of a distributed algorithm involving 3 processes,  $P1$ ,  $P2$ ,  $P3$  and the events  $a1$ ,  $b1$ ,  $c1$ ,  $d1$  on  $P1$ ,  $a2$ ,  $b2$ ,  $c2$ ,  $d2$  on  $P2$ ,  $a3$ ,  $b3$ ,  $c3$  on  $P3$ .

1. Do you think that the way the diagram is depicted relies on the atomic model (introduced in the Mattern paper) ?
2. Compute Lamport clock values for each of the events. Timestamp accordingly the messages exchanged
3. Compute the Vector clock values (vectors with 3 values) for each of the events
4. Comment the values of the vectors that timestamp the events  $c1$  and  $c3$
5. Tell how events  $b3$  and  $c2$  are timestamped using Lamport clocks, and using these clocks tell if you can or not compare  $b3$  and  $c2$  according to the causality ("happened-before") relation.  
Do the same but using vector clocks.  
Do again question 5, but on events  $b3$  and  $d2$ .
6. Describe in terms of events, the cuts (more precisely, the frontiers of the cuts)  $C$ ,  $C'$ ,  $C''$ . Are these cuts consistent ?
7. Given  $r_i$ , the number of messages received by  $P_i$ , and  $s_i$  the number of messages sent by  $P_i$ , for a cut  $C$ . Compute the sum over  $i$  of  $s_i = S$  and the sum over  $i$  of  $r_i = R$ , for each cut  $C$ ,  $C'$ ,  $C''$ .
8. Do the values obtained by the cut  $C''$  enable you to conclude that the algorithm is terminated. ?